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# Phenomenological analysis of the s-d exchange interaction in dilute Cu-Mn alloy at helium temperature

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# ABSTRACT

The S-d exchange interactions in dilute Cu-Mn alloys was studied on concentration (C) varying between 10.5 and 2081.8 ppm of Mn in Cu within the (0.03K–4.2K) temperature range. Using electrical resistivity data on those alloys, the s-d exchange integral ( $J_{sd}$ ), which is negative, has calculated to show a clear dependence on (Ln C). This dependence, confirming thus the dominance of Kondo effect below 1000 ppm impurity concentration, but above this concentration, we expected an interference between Kondo effect and spin glass regime, which mean that spin glass regime has to prevail more than Kondo effect. Copyright © 2014 VBRI press.

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# Introduction

The main objective of this paper is to study the huge effects on the coupling between the dilute magnetic impurities (Mn), which gives rise to the formation of local magnetic moments, and the conduction electrons from the host noble metal (Cu).

Electrical resistivity is a great source of information, especially to get the values of the s-d exchange integral  $J_{sd}$ . For a very dilute alloys (concentration below 100 ppm of Mn), the low-temperature resistivity is dominated by an anomalous Kondo scattering of the conduction electron spin at the local magnetic moments. A typical logarithmic divergence of the resistivity will begin above the Kondo's temperature ( $T_K$ ) until the minimum in the resistivity of Cu-Mn Kondo alloys, where higher temperatures is prevailed, and when the magnetic impurity concentration Increasing until (1 at. %), the interaction between the local magnetic moments and conduction electrons ,which is

governed by the Ruderman-Kittel-Kasuya-Yosida (RKKY) **[1-3]** interaction will form a spin-glass phase **[4]**.

The method, I have used, to calculate  $J_{sd}$  was the analysis of crude experimental data and by simi-emperical simple calculating, I found that the  $J_{sd}$  decreases logarithmically with concentration and gives a very important information about competition between Kondo effect and spin glass regime[5], which need a deeper study in the future.

# Theoretical background

The introduction of few ppm of 3d or 4f magnetic impurity in a non-magnetic matrix leads to an s - d exchange interaction between the spins of the conduction electrons  $S_e$ and the Localized magnetic moment  $S_d$  of the transition element, which can be described by a Hamiltonian:

$$H = J_{sd} S_e S_d + v \tag{1}$$

Where  $(J_{sd})$  is the exchange coupling parameter, and  $\mathcal{V}$  is any ordinary scattering from the ion carrying the local moment. With a negative  $J_{sd}$ , the interaction leads to an increase of localized spin disorder resistivity with decreasing temperature.

The competition between the spin disorder scattering and the phonon exhibits the minimum in the resistivity of this regime **[6-9]**. Phenomenologically; the above competition is mainly manifested at low temperatures in the form:

$$\rho = aT^{5} + c\rho_{m} + c\rho_{1}Ln(T)$$
<sup>(2)</sup>

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Where  $\rho_m$  the spin scattering resistivity, and  $\rho_1 = \rho_m (3ZJ_{sd}) / E_F$ , (*E<sub>F</sub>*=the Fermi energy), (*Z*=number of conduction electrons per atom).

In this work, I endeavour to show the behaviour of  $J_{sd}$  in some Cu – Mn alloys, despite the fact that there is the bulk of information has been put forward on these alloys during and after the 1980s, the electrical resistivity one of many sources to provide a powerful means to trace the s – d exchange interaction dominating these alloys.

# Analysis of data

Matula and others reported crude data [10-12] on electrical resistivity and methods of manufacturing of alloys, especially in respect of purity, constituting the major experimental background in this work. They come from direct measurements already carried on Cu – Mn alloys (and many others noble –transition metals alloys) with concentrations ranging from 10.5 ppm to 2081.3 ppm of Mn in Cu within the (0.03 - 4.2K) range [11-13].

Fig. 1, scales  $\Delta \rho / c$  versus Ln (T/c) give us by suit fitting an expression like a logarithm of power series solution;



Fig. 1.  $\Delta \rho/c\%$  Vs. Ln(T/C%) for Cu-Mn alloys T/C% (k/at%).

$$\Delta \rho / c = a + b \ln T / c + c (lnT / c)^{2} + d (lnT / c)^{3} + e (lnT / c)^{4} + f (lnT / c)^{5} + g (lnT / c)^{6} + h (lnT / c)^{7} + i (lnT / c)^{8} + j (lnT / c)^{9} + k (lnT / c)^{10} + .... + n (lnT / c)^{n}$$
(3)

The first two terms (first- order approximation) show a bold line at figure (1), where pure magnetic resistivity could be defined from that lines as a function of (LnT), and by using a fitting's programming we can find from the ones of the bold lines a relation as following (**Fig. 2**);

$$\Delta \rho = B - A' LnT \quad 10^{-8} \Omega.m \tag{4}$$

This matches with Hamann's expression [13-16];

$$\frac{\Delta\rho(T)}{C} = \left[\frac{\Delta\rho(0)}{2C}\right] \left\{ 1 \pm Ln\left(T/T_{k}\right) / \left[Ln^{2}\left(T/T_{k}\right) + \left(\pi^{2}s\left(s+1\right)\right)\right]^{\frac{1}{2}} \right\}$$
(5)  
where  $+ sign \rightarrow T < T_{k}$   
 $- sign \rightarrow T > T_{k}$ 

 $T_k$  =Kondo temperature

**Fig. 2** expresses exactly what a compatible between experimental relation (4) and theoretical Hamann's expression (5) there are.



Fig. 2.  $\Delta \rho/c\%$  as a function of Ln(T/C%) T/C%.

Definitely, allowing the inclusion of potential scattering effect with single impurity kondo effect, and sharp determination of kondo temperature  $T_k = 36$  mK. Calculated values of J<sub>sd</sub> reveal a variation;

$$J_{sd} = -0.014898811Ln (C) - 0.17956871 \quad ev \quad (6)$$

(C is Mn's concentration in ppm units), as it has shown in Fig. 3.

#### J<sub>s-d</sub>=a+b LnC





Fig. 3. Js-d as a function of Ln(C) for Mn concentration in Cu. C ppm.

Expression (6) was calculated according to a width of internal field distribution [ 12,16 ] at  $T_{max}$  (characterize the maximum value of the resistivity at Fig. 1;

$$\Delta = \delta_{\max} T_{\max} = \frac{J_{sd}^2 c}{E_F}$$
  
$$\delta_{\max} = 0.55 \qquad T_F = 8.10^4 K \tag{7}$$

# **Results and discussion**

As it is shown in Fig. 3, above 850 ppm, our calculation to  $J_{sd}$  leads, just as other works do  $\left[12,\!17\,,\,18\,,\,19,\,20\,\right]$  to believe that magnetic transformation takes place from antiferromagnetic to ferromagnetic state and between 860 ppm and 2000 ppm may be a spin glass regime starts to prevail.

When we come back to Kondo's temperature at Hamann's expression (5), it is most appropriately to denote that the Kondo's temperature given as [21];

$$T_{\rm K} = T_{\rm F} \, \operatorname{Exp}\left(\frac{-1}{n(E_{\rm F})J_{\rm sd}}\right) \tag{8}$$

Where, initially,  $T_F = 8.12 \ 10^4 \text{ k}$ , and n ( $E_F$ ) = 0.294 ev<sup>-1</sup>.

It seems that  $T_k$  is not constant as we noted above, and is not consistent with [22], and has clear dependence on  $J_{sd}$ . Of course, we need more studying to pursue this point.

Finally, as a result, and from Fig. 3, we can classify a Kondo's regime in respect of concentration as following;

- 1. pure kondo regime vanishes at concentration 63 ppm of magnetic impurity (Mn).
- 2. Mixed regime ( kondo + SG ) from 63 ppm to 860 ppm.
- **3**. Ideal spin glass from 860 ppm to about 1%.

# Conclusion

When we increase the concentration of magnetic impurity, The s-d exchange interactions will move to RKKY interactions, where J<sub>sd</sub> will represent a phenomenological order parameter, which reflects a shift of interactions between conduction electrons and localized magnetic moments and discovers the new magnetic transformation from a regime to be other.

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