www.vbripress.com, www.amlett.com, DOI: <u>10.5185/amlett.2012.4332</u>

# On lattice distortion by isovalent cations in silver sulphate solid electrolyte

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Received: 14 April 2012, Revised: 15 May 2012 and Accepted: 18 May 2012

# ABSTRACT

Detailed impedance spectroscopic studies are carried out by incorporating various guest iso-valent cations within the solid solubility limit having different ionic radii in  $Ag_2SO_4$ . The solid solubility limits up to x = 3 mole% cation doped  $Ag_2SO_4$  are set with XRD, SEM, IR and DSC techniques. A major dependence of conductivity on the ionic size of the doped iso-valent cations is observed. The ionic conductivity is found to increase with the incorporation of a guest cation that creates *appropriate* distortion factor in iso-valent cation doped  $Ag_2SO_4$ . The conductivity of  $Ag_2SO_4$  is found to be dependent on the ionic size of the guest cation, particularly in the low-temperature modification of  $Ag_2SO_4$  ( $\beta$ -phase). These results could throw light on the fundamental conduction mechanism in  $Ag_2SO_4$  and also on the criterion of selecting the impurity cation in the classical doping method. The optimized solid electrolytes can then be utilized for their technological applications in electrochemical devices such as  $SO_x$  sensors and thermal batteries. Copyright © 2012 VBRI Press.

Keywords: Lattice distortion; solid electrolytes; silver sulphate; fast ionic conductors.



**S. W. Anwane** obtained Ph.D. degree from Nagpur University in 2000 and is working as Associate Professor in Physics at Shri Shivaji Education Society Amravati's SCIENCE COLLEGE, Congress Nagar, Nagpur. He has worked on Fast Ionic Conductor, Solid Electrolytes, Gas Sensors, Simulation. He has published books on Applied Physics, Electromagnetic Fields. He is recipient of Senior Research Fellowship of Council of Scientific & Industrial Research, New Delhi..

## Introduction

Silver sulphate, a non-alkali metal sulphate, is an exception which shows high cationic conductivity in spite of the bigger size of Ag<sup>+</sup>. It undergoes a structural phase transition from the high temperature highly conducting hexagonal  $\alpha$ phase to the low temperature moderately conducting orthorhombic  $\beta$ -phase at 416°C. It attracted scant attention until its potential application in  $SO_x$  (x=2, 3) galvanic sensors was proved [1]. Recently, ever since the concept of using a metal/metal sulphate reference electrode in solid electrochemical gas sensors has evolved, it has attracted a great deal of attention. It exhibits many advantages over other sulphate-based [2] solid electrolytes in engineering SO<sub>2</sub> gas sensors like: (i) coexistence of Ag–O–S phase in  $Ag/Ag_2SO_4$ ; (ii) equilibration of antagonist  $SO_4^{2-}$  (solid) with SO<sub>2</sub>/SO<sub>3</sub> (gas); (iii) invariance of high ionic conductivity over the  $SO_x$  environment, etc. [3-5]. In contrast to earlier reports [6], our preliminary investigations revealed that in

addition to valency, the ionic size and electronic structure of doped cations do play an important role in ion transport through the solid in low-temperature phases of sulphates [7-**12**]. The solid solubility limit for  $(100-x)Ag_2SO_4$ : (x)Me<sub>2</sub>SO<sub>4</sub> has been established for  $x \leq$  3mole% (Me=Li, Na, K, Rb & Cs). Variation in the parameters like peak frequency, pre-exponential factor, activation energy, ionic conductivity has been studied as a function of lattice distortion (contraction/expansion). The trend has been interpreted on the basis of structural changes caused in the host lattice of Ag<sub>2</sub>SO<sub>4</sub> when Ag<sup>+</sup> is partially replaced by Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>, Rb<sup>+</sup> & Cs<sup>+</sup>. The present work revisits [8] study on role of electronic structure and the influence of lattice distortion caused by iso-valent cations) on the mobility of  $Ag^+$  in orthorhombic  $\beta$ - $Ag_2SO_4$  to understand the fundamental conduction mechanism and simultaneously to obtain an apt silver sulphate based material for SO<sub>2</sub> gas sensor. A detailed structural analysis based on XRD, SEM, IR confirms the solid solubility limits of the monovalent sulphates in the host  $\beta$ -Ag<sub>2</sub>SO<sub>4</sub>.

A fine analysis of lattice distortion has been carried out to understand its effect on conductivity of the newly synthesized solid electrolyte material. Comprehensive impedance analysis has been carried out to understand the lattice distortion contribution in governing conductivity and activation energy. Polynomial of 3<sup>rd</sup> order has been explored in governing role of factors expanding/contracting the lattice for its correlation with the conductivity and activation energy. Investigations on lattice distortion in superconducting phase/super ionic conductors have been explored by various workers [**13-15**].

# Experimental

The initial ingredients  $Ag_2SO_4$ ,  $Me_2SO_4$  where Me=Li, Na, K, Rb, Cs; with assay more than 99.99% were procured from Aldrich Chemicals (USA). These pre-dried initial ingredients with mole fractions  $(100-x)Ag_2SO_4:(x)Me_2SO_4$  (where x=0-7 mole%), were mixed in an agate mortar under acetone for 2 hrs. The compositions were filled in translucent quartz ampoules (to avoid photo decomposition of  $Ag_2SO_4$ ) and were heated in an electric furnace to a temperature 20°C above the melting-point. Later, the melt was allowed to crystallize by cooling at a cooling rate of  $1.5^{\circ}$ C/min. The ingots, obtained by breaking the ampoules, were pulverized to get a fine powder.

The prepared samples were characterized by X-ray powder diffraction (XRD) (Philips PW1700 diffractometer attached with PW 1710 controlling unit) using CuK<sub> $\alpha$ </sub> radiation. The solid–solid phase transition temperature and the heat of transition were studied by Differential Scanning Calorimetric (DSC) using Mettler TA 4000, DSC 25 at a heating rate of 10°C/min. The microstructures were examined with the help of Scanning Electron Microscope (SEM) (Cambridge 250 Mark-III stereoscan electron microscope). Using InfraRed (IR) spectroscopy, the stack plots of the samples were recorded in several spectral regions of interest using a Perkin-Elmer 983 IR spectrometer.

For electrical characterization, the specimens were obtained in the form of circular discs of 9mm diameter and 2mm thickness by pressing the powder with the help of a Specac (UK) stainless steel die-punch and hydraulic press. The pellets so obtained were sintered at 500°C for 24 hrs. Prior to spring loading of the pellets between silver electrodes, a good ohmic contact was ensured by using a quality silver paint on both opposite parallel surfaces of the pellet, followed by baking at 200°C for 2 hrs. Preceding the impedance measurement, the spring-loaded sample was heated to 510°C for an hour to homogenize the charge carriers in the sample and simultaneously to remove the moisture content therein. Later, the temperature of the furnace was reduced in step of 20°C at a cooling rate of 2°C/min. At the end of each cycle the sample was allowed to attain thermal equilibrium for a dwell time of 30 minutes using a Eurotherm 810 PID temperature controller. At the end of each dwell time, the real and imaginary parts of the impedance were measured as parametric functions of frequency in the range 5Hz-13MHz and temperatures from 510 to 100°C during the cooling cycle using an HP 4192A IF impedance analyzer. The entire measurement system was properly shielded to avoid external electrical pickups. A stainless steel faraday cage was employed for this purpose. The ionic transference number of the specimens was measured by Wagner's dc polarization method using a Keithley SMU 236 with cell configuration: Ag/Electrolyte/Pt.

A small dc potential was applied across the above configuration to record current at zero and saturation time to know the current under polarized and un-polarized current to obtain the ionic transference number.

$$t_i = \frac{\sigma_0 - \sigma_\infty}{\sigma_0}$$

The reproducibility of the impedance data and transference number was confirmed by repeating the measurement on freshly prepared samples.

## **Results and discussion**

Structural characterization forms the very basis for understanding the structure correlated conduction mechanism **[16-22]**.

# X-ray powder diffraction

The XRD pattern for all five systems was obtained at room temperature. Up to x=3 mole%, the lines corresponding to the guest cation are absent while a small intensity for Me<sub>2</sub>SO<sub>4</sub> starts appearing for x > 3 mole% concentrations and above. This indicates that up to x=3 mole% Me forms solid solution with Ag<sub>2</sub>SO<sub>4</sub>. A comparison of experimental, *d*, and relative intensity values,  $I/I_0$ , with those of JCPDS data is given in **Table 1**.

**Table 1.** A comparison of experimental d and  $I/I_0$  values with JCPDS data for (97)Ag<sub>2</sub>SO<sub>4</sub>:(3)Me<sub>2</sub>SO<sub>4</sub> in orthorhombic phase.

Me	Me=Li		Me=Na		Me=K		Me=Rb		Me=Cs		JCPDS data for Pure Ag <sub>2</sub> SO <sub>4</sub>		
d (Å)	1/10	d (Å)	1/10	d (Å)	1/0	d (Å)	<i>i</i> /i0	d (Å)	i/10	d (Å)	1/10	[hkl]	
4,694	7	4.702	8	4,697	8	4.698	7			4.699	10	[111]	
3987	20	3985	11	3.950	19	3.955	20	-	•	3.994	25	[220]	
3171	59	3171	29	3177	71	3.178	68	3.177	59	3.177	70	[040]	
2871	100	2.873	100	2876	10	2.875	100	2.878	100	2.873	100	[311]	
2642	48	2,648	31	2645	54	2,646	54	2.647	55	2.644	90	[022]	
2.415	23	2.481	12	2.421	25	2.421	24	2.425	32	2.421	30	[311]	
1926	17	1923	18	1926	24	1.927	26		•	1.926	30	[351]	
1708	14	1713	8	1710	20	1.711	19		•	1.712	17	[062]	

It is clearly evident that in the case of  $3mole\% Me_2SO_4$ added to  $Ag_2SO_4$  the *d* values in XRD patterns are slightly deviated from the JCPDS data of  $\beta$ -Ag<sub>2</sub>SO<sub>4</sub> (Table 1). This small deviation in experimental d(Å) values can be attributed to the partial replacement of Ag<sup>+</sup> by wrong-sized Me<sup>+</sup>. Further, no decomposition appears from the XRD data. The absence of any line corresponding to either Me<sub>2</sub>SO<sub>4</sub>, AgMeSO<sub>4</sub> or any other intermediate phase for 3mole% Me<sub>2</sub>SO<sub>4</sub> added to Ag<sub>2</sub>SO<sub>4</sub> indicates solid solubility (SS). In case of (95) Ag<sub>2</sub>SO<sub>4</sub>:(5) Me<sub>2</sub>SO<sub>4</sub> added to Ag<sub>2</sub>SO<sub>4</sub>, few meager lines corresponding to Me<sub>2</sub>SO<sub>4</sub> appear which may be attributed to the advent of precipitation following its in situ dispersion in the host Ag<sub>2</sub>SO<sub>4</sub> (SS). A closer look at Table 1 reveals that, in general, there is a slight shift (negative) in d(Å) values for the systems where the dopant ion size is smaller than that of Ag<sup>+</sup>, such as Li<sup>+</sup> and Na<sup>+</sup>, whereas the shift is positive in d(Å) values for dopants with relatively bigger-size cations, such as  $K^+$ ,  $Rb^+$  and  $Cs^+$ . The local lattice distortion caused by the 'wrong'-size cation substitutions was further investigated to detect the magnitude of the distortion. This lattice distortion which has a primary indication of small shift in 'd' value has been further investigated to find the change in lattice volume and its effect on ionic conductivity.

A closer look at **Table 2** reveals that the cell volume undergoes a continuous contraction for  $Li^+$  and  $Na^+$ ; whereas it undergoes a continuous expansion for  $K^+$ ,  $Rb^+$ substitution. These results and Cs (lattice contraction/expansion on the substitution of the smaller/bigger alio-valent cations (Table 2)) are suggestive of the fact that that lattice distortion (expansion and contraction) is directly governed by the 'distortion factor',  $R_{\rm g}/R_{\rm h}$ ,  $R_{\rm g}$  and  $R_{\rm h}$  being the ionic radii of the guest and host cations, respectively. The lattice cell volume for (97)Ag<sub>2</sub>SO<sub>4</sub>:(3)Me<sub>2</sub>SO<sub>4</sub> has been calculated and volume distortion factor  $V_g/V_h$  has been presented in **Table 2**. It clearly reveals that the ionic radius of smaller/grater size causes lattice contraction/expansion. Moreover, electronegativity (according to Pauling) and outer electron shell is also displayed in the table for an overview.

System/Para meters	Me =Li	Me =N	Me =A	M e= K	Me =R b	Me =C
a	10. 221	<b>a</b> 10. 22	<b>g</b> 10. 26	10. 27	10. 241	<b>s</b> 10. 26
Lattice Paramete rs b	12. 682	7 12. 68 6	9 12. 70 6	1 12. 72 6	12. 714	7 12. 73 7
С	5.7 53	5.7 5	5.8 18	5.8 23	5.8 53	5.8 41
Cell Volume	745 .71 95	74 6.0 03 4	75 9.1 20 5	76 1.1 05	762 .08 44	76 3.8 32 1
Ionic Radius R of cation (nm)	0.0 6	0.0 95	0.1 33	0.1 44	0.1 49	0.2 67
$\frac{R_g}{R_n}$	0.4 511	0.7 14 2	1.0 00 0	1.0 82 7	1.1 203	2.0 07 5
$\frac{V_g}{V_h}$	0.9 823	0.9 82 7	1.0 00 0	1.0 02 6	1.0 039	10 06 2
Electro- negativity (Pauling)	1	0.9	0.8	1.9	0.8	0.7
Outer Shell	$2s^1$	3s <sup>1</sup>	$4s^1$	$5s^1$	5s <sup>1</sup>	6s <sup>1</sup>

**Fig. 1** represents the variation of normalized volume distortion  $\binom{V_g}{V_h} - 1$  with normalized cation size  $\binom{R_g}{R_h} - 1$  which we shall call distortion coefficient. The trend of data points clearly indicates that as the size of guest cation (distortion coefficient) doped is increased/decreased the volume (normalized) accordingly increases/decreases. This can be clearly attributed to expansion and contraction of the lattice. Further second degree polynomial fit of the data points has been obtained to understand the non-linear behavior exhibited. The second degree polynomial fitted with R-squared value 0.888 governed by equation.

$$\left(\frac{V_g}{V_h} - 1\right) = -0.017 \left(\frac{R_g}{R_h} - 1\right)^2 + 0.027 \left(\frac{R_g}{R_h} - 1\right) \dots (1)$$

here in the given host silver sulphate lattice, the doping causing volume expansion is governed by coefficient 0.027 while the contraction by -0.017. The empirical formula (1) developed helps in interpolations/extrapolations over and around the data points. It possesses local maxima at (0.794, 0.0107).

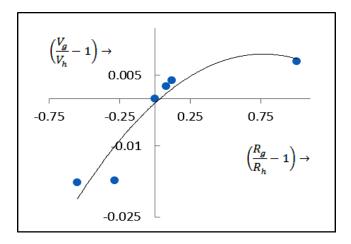


Fig. 1. Plot of normalized lattice distortion coefficient versus normalized volume distortion in Orthorhombic phase.

#### Differential scanning calorimetry (DSC)

Differential Scanning Calorimetric (DSC) and Infra Red (IR) studies were carried out on all samples. It was observed that for x=0, 0.5, 1, 3 mole % the DSC isotherms, transition temperature, enthalpy etc remained same. The Infra-red spectrums are also identical for x=0, 0.5, 1, 3 mole% leaving the frequency nodes unchanged. A DSC isotherm and IR spectrum for the sample x=0 are depicted in **Fig. 2**.

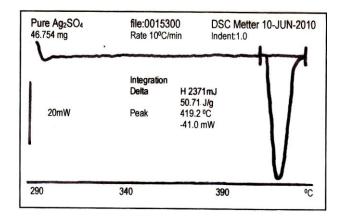


Fig. 2. DSC isotherm for pure Ag<sub>2</sub>SO<sub>4.</sub>

The phase transition temperature and heat of transition obtained from the thermograms of Me=Cs added samples has been presented in **Table 2**. It is evident from the **Table 2** that the transition temperature decreases like in many cases [23-26] with addition of impurity within solid solution region. Absence of additional peak in the thermogram indicates that no other phase is present.

Table 2. DSC Data for (100-x)Ag<sub>2</sub>SO<sub>4</sub>:( x)Cs<sub>2</sub>SO<sub>4</sub>

Sample composition	J/gm	T °C
x=0	50.7	429.2
x = 0.5	51.7	427.5
<i>x</i> =1	55.9	429.5
<i>x</i> =3	24.0	429.2
<i>x</i> =5	49.7	429.5

The decrease in phase transition temperature may be due to the partial replacement of host cation by the guest. Such partial replacement resulting due to the formation of solid solution that gives raise to additional strain energy caused by local elastic distortion. The additional strain energy is considered to be main factor responsible for promoting the solid-solid phase transition to occur at relatively lower temperature as compared to host system.

Table 3. Frequencies (cm  $^{-1})$  for composition with small size and big size cation in  ${\rm Ag}_2 SO_{4.}$ 

Wa ve No/ com			Me=L	i	Me=Rb			
posi tion	x= 0	<i>x</i> = 0.5	<i>x</i> =1	<i>x</i> =3	<i>x=</i> 0. 5	<i>x</i> =1	<i>x</i> =3	
$\nu_1$	98	98						
	3	0	980	981	984	987	989	
$v_2$	46	46						
	6	7	482	485	471	472	468	
$v_3$	11	11	111	112	112	112	112	
	23	21	6	1	5	7	8	
$\nu_4$	61	61						
	9	7	617	618	618	617	620	

#### Infrared spectroscopy (IR)

Various frequencies obtained from the infrared spectra of a number of compositions including that of pure  $Ag_2SO_4$  are compared with the standard spectra of  $Ag_2SO_4$  in **Table 3** to understand the role played by the impurity cation *vis-a-vis* the  $Ag_2SO_4$  structure. **Fig. 3** indicates Infra-Red spectrum for pure  $Ag_2SO_4$ . **Table 3** indicates wave number and transmittance nodes. It clearly shows a negligible change for concentrations up to 3 mole %.

**Table 3** shows the fundamental frequencies of  $SO_4^{2-}$  having  $T_d$  symmetry occurring at  $v_1$ ,  $v_2$ ,  $v_3$  and  $v_4$  respectively, the symmetric stretching (Raman active), doubly degenerate bending (IR active) and the doubly degenerate anti-symmetric (IR and Raman active frequencies)).

These frequencies are in closed agreement with the earlier reported [**27-28**] for  $SO_4^{2-}$  of  $Ag_2SO_4$ . Energy consideration (mainly electrostatic and thermodynamic) suggests the splitting of degenerate modes which depend on cations; it increases with increase in ionic radii, ionic polarizability and cation oxygen distance for isomorphous sulphate. No other additional frequencies other than those corresponding to  $Ag_2SO_4$  are observed.

It rules out the possibility of precipitation or formation of intermediate phase. These results strongly support XRD results discussed in preceding sections. Moreover, it can be seen from the data that  $v_1$  and  $v_3$  shift to the lower values when Ag<sup>+</sup> is replaced by small size Li<sup>+</sup>. On the other hand  $v_1$  and  $v_3$  shift to the higher values when Ag<sup>+</sup> is replaced by large size Rb<sup>+</sup>.

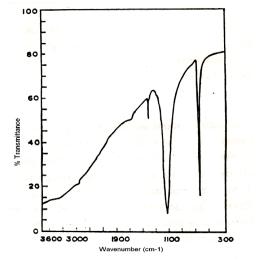
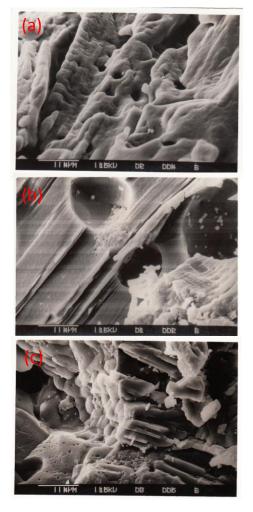


Fig. 3. Infra Red Spectrum for pure Ag<sub>2</sub>SO<sub>4</sub>



**Fig. 4.** Microphotographs of (100-x)Ag<sub>2</sub>SO<sub>4</sub>:( x)Rb<sub>2</sub>SO<sub>4</sub> with (a) x=0, (b) x=3 and (c) x=5 mole%.

#### Scanning electron microscopy (SEM)

The formation of solid solubility of various cations in Ag<sub>2</sub>SO<sub>4</sub> is further confirmed by the evidences obtained by characterizing the samples using SEM. **Fig. 4** representing microphotographs of (100-x)Ag<sub>2</sub>SO<sub>4</sub>:(x)Rb<sub>2</sub>SO<sub>4</sub> with (a) x=0, (b) x=3 and (c) x=5 mole% reveals that the grain morphology of the host material is more or less unaffected by an addition up to x=3 of Rb<sub>2</sub>SO<sub>4</sub>. On the other hand, a few traces of insoluble Rb<sub>2</sub>SO<sub>4</sub> are visible in **Fig. 4**(*c*) for samples with x=5. Similar results are found in other monovalent systems. These results suggest that a complete solid solution can be ensured only up to 3 mole% of Me<sub>2</sub>SO<sub>4</sub> in room temperature orthorhombic phase.

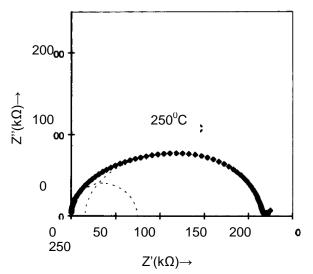


Fig. 5. Complex impedance plot for pure  $Ag_2SO_4$  at 250 °C (the doted line represents the best fit curve)

#### Impedance analysis

The results of complex impedance spectroscopy are critically analyzed to find bulk properties by eliminating extraneous parameters such as electrode polarization and grain boundary. A distorted semicircular arc is observed for the pure sample (**Fig. 5**). A closer look at this figure reveals that the distorted semicircular arc is a combination of two overlapping depressed semicircular arcs. On the other hand, a single semicircular arc is seen for K<sup>+</sup>, Rb<sup>+</sup> and Cs<sup>+</sup> which is attributed to the limitation of the upper sweep frequency (13MHz). However, there are two discernible semicircular arcs in the case of the rest of the samples.

Since the conductive silver coating on both the surfaces of the electrolyte acts as a reversible (nonblocking) electrode, no electrode polarization is reflected in the complex impedance plane. A non-linear least squares (NLS) fit method is used to ascertain the presence of two overlapping depressed semicircular arcs. In order to accomplish this, the complex impedance data acquired at a fixed temperature using a computer controlled HP 4192A IF impedance analyzer is fitted to the following equation using our software developed in Turbo C.

$$Z = Z(0) + \frac{Z(\infty) - Z(0)}{1 + (j\omega\tau)^{\alpha}} \qquad ...(2)$$

where Z(0) and  $Z(\infty)$  are limiting values of  $Z(\omega)$  when  $\omega$  varies from minimum to maximum,  $\tau$  is relaxation time,  $\alpha$  is empirical measure of departure from ideal Debye model. During the NLS fitting the sum of squares is minimized by unity weighting represented by

$$S_i = (\Delta R_i)^2 + (\Delta I_i)^2 \qquad \dots (3)$$

where  $\Delta R_i$  and  $\Delta I_i$  are the real and imaginary fitting residuals. The presence of two overlapping depressed semicircular arcs is suggestive of the occurrence of two prominent conduction mechanisms simultaneously under the external perturbation ac signal. Various interpretations can be made in the impedance analysis in a polycrystalline ion conducting specimen; however, an experimental impedance obviously contains major contributions from inter-grain and intra-grain ion migration [29-30]. In order to have a more meaningful discussion, the voluminous impedance data obtained by following the above procedure are fitted in using the equation

$$f_p = f_0 e^{\frac{-E_m}{kT}} \qquad \dots (4)$$

The peak frequency of the complex impedance

$$\omega_{max} = 2\pi f_p$$

$$\frac{1}{\tau} = \frac{1}{RC} = \frac{\sigma}{\varepsilon \alpha \mu C}. \quad \mu = \mu_0 e^{\frac{-E_m}{kT}} \qquad \dots (5)$$

where  $\mu$  is the cationic mobility,  $E_m$  denotes the migration enthalpy,  $\mu_0$  is proportional to the jump attempt frequency, and k and T are the Boltzmann constant and temperature in K. The frequency fp derived from  $\omega_{max}$  is an effective averaged hopping frequency of an ion. The effective prefactor  $f_0$  depends on the defect charge carrier density, C.

The process of ion migration through the sample involves the activation energy for migration of ions across the grain boundaries,  $E_{a2}$  (obtained from the semicircle corresponding to high frequency) and that for migration of ions within grain (intra-grain) ion migration,  $E_{a1}$  (obtained from the semicircle corresponding to low frequency). Evidently, the partial replacement of the host Ag<sup>+</sup> by dopant cations within the grain alters the local environment leaving the grain boundary undisturbed. This alteration in the local environment modifies the activation enthalpy for intra-grain ion migration, whereas that for inter-grain conduction remains invariant. Similar results are found in case of the iso-valent cation doped Li<sub>2</sub>SO<sub>4</sub> [**31**].

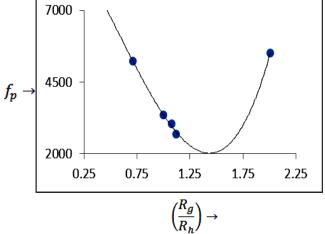
In the complex impedance plot real and imaginary impedance has been plotted as a parametric function of frequency. It indicates a depressed semicircular arc and for the series of interest the peak frequency has been plotted with relative ionic radius. It also exhibits a trendy behavior as shown in **Fig. 6**.

The given data points for relative ionic radius with  $f_p$  has been least square fit to third degree polynomial with R-squared value 0.998;

$$f_p = 3392 \left(\frac{R_g}{R_h}\right)^3 - 5957 \left(\frac{R_g}{R_h}\right)^2 - 3819 \left(\frac{R_g}{R_h}\right) + 9744 \qquad \dots (6)$$

The R-squared value 0.998 confirms third degree polynomial Eq (6) encompasses trend of data points in the **Fig.6** which reveals the peak frequency in complex impedance plot also depend upon the distortion coefficient  $\left(\frac{R_g}{R_h}\right)$ . The coefficients arising in the equation are governing lattice distortion factors supporting and opposing ion

migration that varies with the lattice expansion and contraction.



**Fig. 6.** Plot of relative ionic radius versus  $f_{\rm p.}$ 

#### Ionic conductivity

The generalized perception of Arrhenius theory of the temperature effect on the reaction rate (ion diffusion) originated from the temperature effect on the equilibrium constant. It is known that:

$$\frac{d\ln(K)}{d\frac{1}{T}} = -\frac{H}{R} \qquad \dots (7)$$

where K is an equilibrium constant, R is the gas constant, and H is the heat of reaction. The equilibrium constant is  $=\frac{k_1}{k_2}$ , where  $k_1$  and  $k_1$  are the rate constants for the forward and reverse reactions respectively. Thus, we obtain;

$$\frac{d\ln(k_1)}{d\frac{1}{T}} - \frac{d\ln(k_2)}{d\frac{1}{T}} = -\frac{H}{R} \qquad \dots (8)$$

Arrhenius recognized that the last equation could be conveniently divided into two parts, each having the form of:

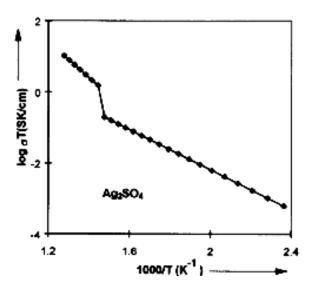
$$\frac{d\ln(k)}{d\frac{1}{T}} = -\frac{E}{R} \qquad \dots(9)$$

where E is referred by Arrhenius as representing the energy difference between the reactants and an activated species. The term E is, therefore, called the activation energy. Taking E as a constant the last can be integrated to yield:

$$ln(k) = ln(A) - \frac{E}{RT}$$

where ln(A) is the constant of integration and the last equation can be converted to:

$$k = Ae^{-\frac{L}{RT}} \qquad \dots (10)$$



**Fig. 7**. Arrhenius plot for pure  $Ag_2SO_4$  in  $\alpha$  and  $\beta$  phases.

This form of equation (10) is the most widely adopted form of the Arrhenius equation. The temperature dependent ionic conductivity in all specimens is governed by Arrhenius equation can be expressed as equation (11);

$$(\sigma T) = (\sigma T)_o exp\left(\frac{E_a}{2KT}\right) \qquad \dots (11)$$

The pre-exponential factor  $(\sigma T)_o$  in the above equation (which is appearing out of constant of integration) is related to the frequency of ionic collisions in the collision theory and to the entropy term in the transition state theory. The equation governs forward and reverse reaction contributing to ionic conductivity ( $\sigma T$ ) and predomination of each other. Arrhenius plots for all the compositions are found to obey the Arrhenius law (11) in both the  $\alpha$  and  $\beta$ phases (as an example, **Fig. 7** depicts this behaviour for the host Ag<sub>2</sub>SO<sub>4</sub>).

The observed change in slope at 416°C with an order of magnitude jump in conductivity in the case of pure Ag<sub>2</sub>SO<sub>4</sub> accounts for the orthorhombic  $\beta$  to hexagonal  $\alpha$ phase transition (**Fig. 5**). The magnitudes of the conductivities (2.22×10<sup>-5</sup> S/cm at 250°C and 3.4×10<sup>-3</sup> S/cm at 440°C) and the transition temperature (416°C) are in close agreement with earlier reports [**32-35**].

#### Concentration dependent conductivity

The concentration of mobile charge carriers in a Frenkel type ionic solid is given by

$$n = \sqrt{k_f} exp\left(\frac{\Delta S_{th} + \Delta S_{cf}}{2k} - \frac{E_f}{kT}\right) \qquad \dots (12)$$

where  $k_f$ ,  $\Delta S_{th}$ ,  $\Delta S_{cf}$  and  $E_f$  are, respectively, the mass action constant, thermal entropy, configurational entropy and defect formation enthalpy. If the system under consideration (solid solution of Ag<sub>2</sub>SO<sub>4</sub> with Me<sub>2</sub>SO<sub>4</sub>) is assumed to be homogeneous and isotropic, then the term  $\Delta S_{cf}$  remains invariant with respect to the distribution of cations and anions, whereas the immediate ions surrounding Me<sup>+</sup> will have a different vibrational frequency (v) from those at regular undistorted sites v. The thermal entropy term,  $\Delta S_{th}$  in the last equation will be a consequence of the change in frequency of the lattice vibration due to the distortion taking place. Considering the Einstein model we may assume that in the doped crystal, each atom neighboring Me<sup>+</sup> is equivalent to three harmonic oscillators each of frequency  $\nu' \neq \nu$ . Then one finds for the increase in thermal entropy per Me<sup>+</sup> the expression,

$$\Delta S_{th} = 12k \log\left(\frac{\nu}{\nu}\right) \qquad \dots (13)$$

substitution of which in last equation (12) leads to:

$$n = k_f \left(\frac{\nu}{\nu}\right)^6 exp\left(-\frac{E_f}{2kT}\right) \qquad \dots (14)$$

This reduces the mobile charge carrier (Ag<sup>+</sup>) concentration, *n*. This is reflected in the conductivity behaviour (a decrease in conductivity) in the cases of Na<sup>+</sup> and Li<sup>+</sup> doped samples (Fig. 8c). The opposite behaviour is expected if  $R_g > R_h$  in which case lattice loosening occurs. Such an expansion opens the lattice in the vicinity of Me<sup>+</sup> thereby widening the window (opening) between the two energetically equivalent cationic sites through which the ion undergoes successive jumps from an occupied site to the vacant site. Cs<sup>+</sup> has  $R_g \gg R_h$  such that the lattice undergoes expansion but beyond a critical value, the wrong-sized dopant ion hinders the mobility of Ag<sup>+</sup>, thus reducing the conductivity (**Fig. 8c**).

Nevertheless, in the case of  $Li_2SO_4$  added to  $Ag_2SO_4$ , in spite of the lattice contraction the lattice opening of the host is large enough for the added  $Li^+$  that it itself can move from one site to a nearby vacant site, i.e., the added  $Li^+$  becomes the mobile charge carrier.

Additionally, coupling of  $Ag^+-Li^+$  helps in the enhancement of the conductivity; the net effect is such that in spite of the lattice contraction, in the case of  $Li^+$  doped  $Ag_2SO_4$ , the conductivity is marginally enhanced. The observed insignificant decrease in conductivity (Na<sup>+</sup> doped  $Ag_2SO_4$ ) is understandable because with the addition of Na<sup>+</sup> the total mobile charge carrier density remains the same. A small decrease in conductivity due to partial replacement of  $Ag^+$  by Na<sup>+</sup> has also been observed by Secco et al [**36-40**]. Rb<sup>+</sup> cation causes optimum lattice expansion that offers optimum ionic conductivity.

#### Lattice distortion dependent conductivity

As seen in **Fig. 8a** and **b**, the conductivity is optimized in the  $\beta$ - and  $\alpha$ -phases for x = 3mole% in the case of Li, Na, K, Rb and Cs doping, whereas the conductivity is found to decrease slightly with concentration for Na doped Ag<sub>2</sub>SO<sub>4</sub>. The Cs<sup>+</sup> doping decreases the conductivity in  $\beta$ -Ag<sub>2</sub>SO<sub>4</sub>. A closer look at the figure clearly reveals that the Rb<sup>+</sup> doped sample gives the maximum conductivity in both phases. Interestingly, the Li<sup>+</sup> doped samples have conductivities comparable to that of the pure host system. When Ag<sup>+</sup> is partially substituted by Me<sup>+</sup>, a lattice distortion (increased entropy) occurs, in general, affecting the mobility of the cation in the host lattice. Particularly, a localized lattice contraction takes place if  $R_g < R_h$  (such as Na<sup>+</sup> and Li<sup>+</sup> replacing Ag<sup>+</sup>), and the lattice expands if  $R_g > R_h$  (such as K<sup>+</sup>, Rb<sup>+</sup> or Cs<sup>+</sup> replacing Ag<sup>+</sup>) as substantiated by the experimental facts.

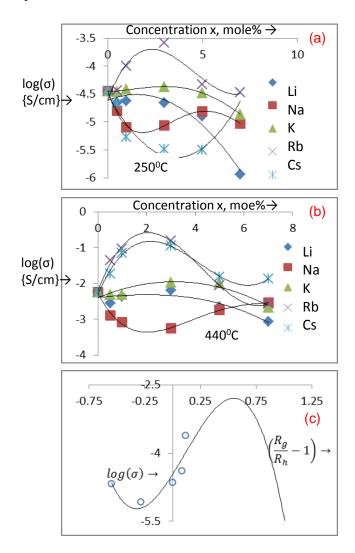


Fig. 8. Variation of  $\log(\sigma)$  with *x* for  $(100-x)Ag_2SO_4:(x)Me_2SO_4$  [Me=Li, Na, K, Rb, Cs] at (a) 250°C, (b) 440°C, (c) with normalized lattice distortion.

The variation of ionic conductivity of (97)Ag<sub>2</sub>SO<sub>4</sub>: (3)Me<sub>2</sub>SO<sub>4</sub> for Me=Li, Na, Ag, K, Rb and Cs has been plotted as a function of lattice distortion factor  $\left(\frac{R_g}{R_h} - 1\right)$ .

The way lattice volume has undergone a trendy contraction and expansion, conductivity has also undergone a trendy change. This change has been least square fit with third degree polynomial as depicted below with R-squared value 0.881.

$$log(\sigma) = -7.358 \left(\frac{R_g}{R_h} - 1\right)^3 + 2.488 \left(\frac{R_g}{R_h} - 1\right)^2 + 3.902 \left(\frac{R_g}{R_h} - 1\right) - 4.469$$
...(15)

The empirical formula (15) developed helps in interpolations/extrapolations over and around the data points. It possesses local maxima at (0.548,-2.79).

This pre-exponent appearing in the equation has been calculated for all system and for  $97Ag_2SO_4$ : $3Me_2SO_4$  it has been studied as it how relates to lattice distortion. The trend of the pre exponential factor with relative lattice volume has been depicted in **Fig. 9**.

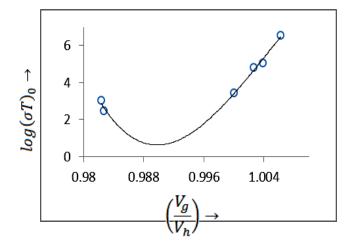


Fig. 9. Plot of relative lattice volume versus  $log(\sigma T)_{0.}$ 

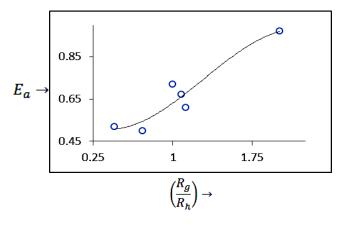


Fig. 10. Relative ionic radii vs. activation energy.

A third degree polynomial is fitted in the given data quite accurately that the R-squared value is 0.986 i.e. close to 1. The polynomial has been found as;

$$log(\sigma T)_o = -79703 \left(\frac{v_g}{v_h}\right)^3 + 2 \times 10^6 \left(\frac{v_g}{v_h}\right)^2 - 2 \times 10^6 \left(\frac{v_g}{v_h}\right) + 80684$$
...(16)

The activation energy (**Fig. 10**) which is superposition of forward and reverse reaction of ion migration through lattice for the series of interest has been studied as a function of relative ionic size of doped cation. The relative ionic size with activation energy has trend of non-linear increase as size of doped cation increased. The third degree polynomial least square fitting for R-squared value 0.901 is;

$$E_{a} = -0.177 \left(\frac{R_{g}}{R_{h}}\right)^{3} + 0.685 \left(\frac{R_{g}}{R_{h}}\right)^{2} - 0.478 \left(\frac{R_{g}}{R_{h}}\right) + 0.601 \dots (17)$$

The empirical formula can be utilized to interpolate and extrapolate the effect relative lattice volume on the pre-exponential factor and provides lattice coefficients arising due to lattice distortion factors on the pre-exponential factor. In the lattice contraction region the curve has negative slope while in lattice expansion it possesses positive slope but with having minima at  $\begin{pmatrix} V_g \\ V_h \end{pmatrix} = 0.989$ .

#### Conclusion

The ionic conductivity is found to increase with the incorporation of a guest cation that creates *appropriate* distortion factor,  $\left(\frac{R_g}{R_h}\right)$ , in iso-valent cation doped Ag<sub>2</sub>SO<sub>4</sub>.

The increase in conductivity in the doped  $Ag_2SO_4$ , despite having  $R_g < R_h$ , is due to the probable role played by the lattice distortion. The conductivity of Ag<sub>2</sub>SO<sub>4</sub> is found to be dependent on lattice distortion caused by the ionic size of the guest cation, particularly in the low-temperature modification of  $Ag_2SO_4$  ( $\beta$ -phase). The optimum conductivity is obtained for x=3 mole% which forms solid solution of Li, Na, K, Rb & Cs in host Ag<sub>2</sub>SO<sub>4</sub>. The preexponential factor, conductivity, activation energy, peak frequency has been optimized with lattice distortion factor caused by mis-match of ionic radius. An empirical equation for optimization using non-linear-least square fit method has also been obtained to understand the trend for generalization. These results could throw light on the fundamental conduction mechanism in Ag<sub>2</sub>SO<sub>4</sub> and also on the criterion of selecting the impurity cation in the classical doping method. The optimized solid electrolytes can then be utilized for their technological applications in electrochemical devices such as SO<sub>x</sub> sensors and thermal batteries.

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